

PRACTICE 1 Exercise 1
COMPUTATIONAL STRUCTURAL MECHANICS AND DYNAMICS
 Marcos Boniquet Aparicio

It's chosen a problem type: *Plane_State*.

Material, self weight condition, and constraints are settled.

The material chosen for the unique surface defined by the four sides has the following properties:

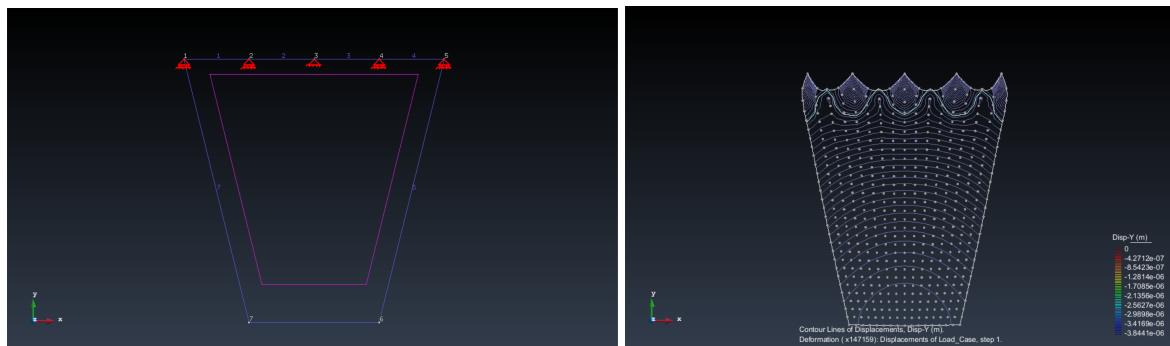
$$E=2,1 \times 10^{11} \text{ Pa}$$

$$\nu=0,3$$

$$\gamma=70000 \text{ N/m}^3$$

$$\text{thickness}=0,10 \text{ m}$$

The constraints as settled as demanded. A preliminary check is done with the highest demand models, this is 9-node quadrilateral and 6-node triangle.



The finest mesh is chosen, being 8x14, delivering a maximum of 980 DoF *structurate* mesh, with good proportions between sides of elements.

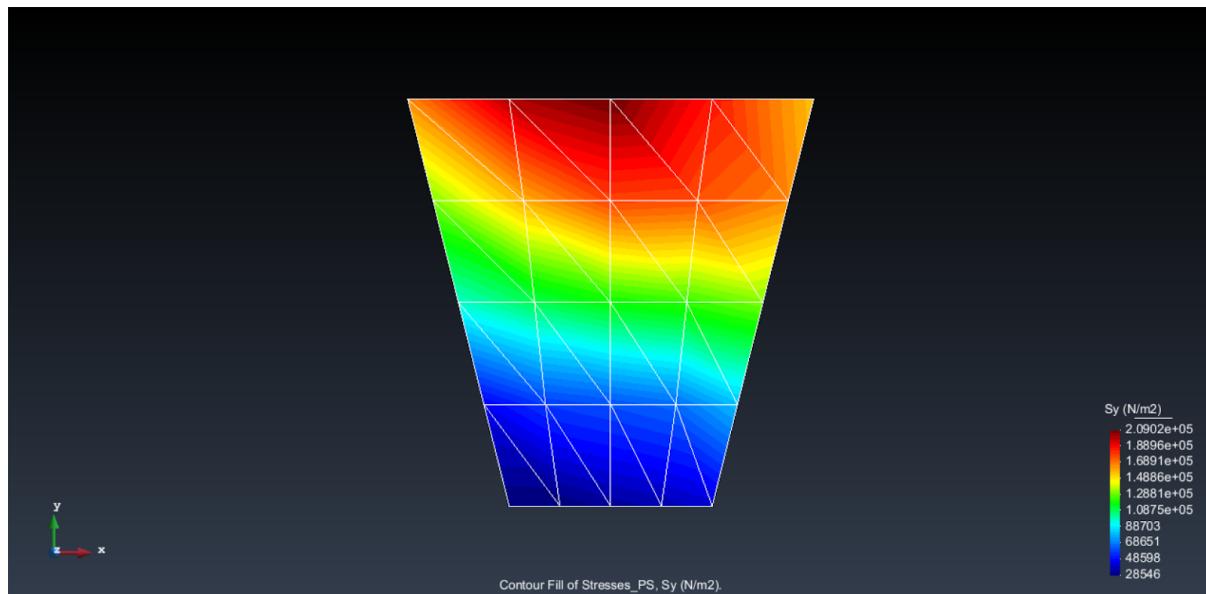
Two more meshes are defined, 4x4, and 4x8.

| ELEMENT TYPE | MESH1 | MESH2 | MESH3 | DoF_1 | DoF_2 | DoF_3 |
|----------------------|-------|-------|-------|-------|-------|-------|
| 3-nodeTriangle | 4X4 | 4X8 | 8X14 | 44 | 84 | 264 |
| 6-node Triangle | | | | 156 | 300 | 980 |
| 4-node quadrilateral | | | | 44 | 84 | 264 |
| 8-node quadrilateral | | | | 124 | 236 | 756 |
| 9-node quadrilateral | | | | 156 | 300 | 980 |

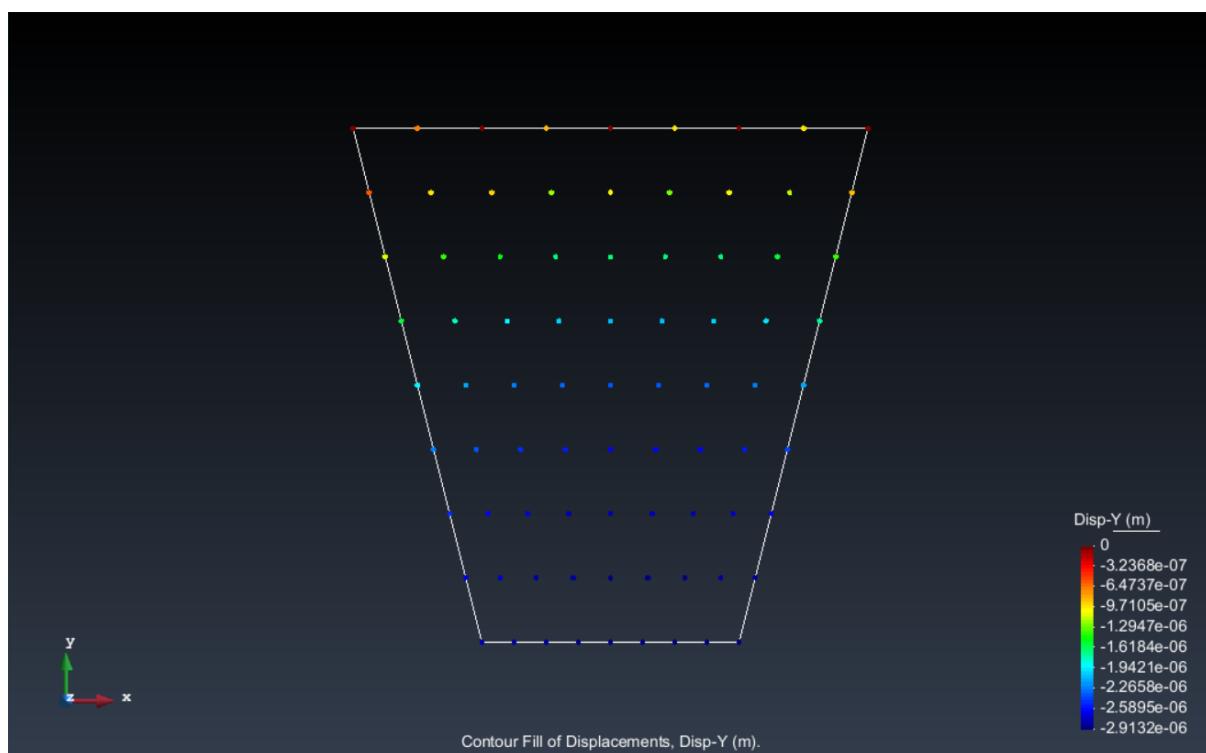
The results of stress and displacements for each of the element type are shown for the mesh, as followed:

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3-NODE TRIANGULAR:

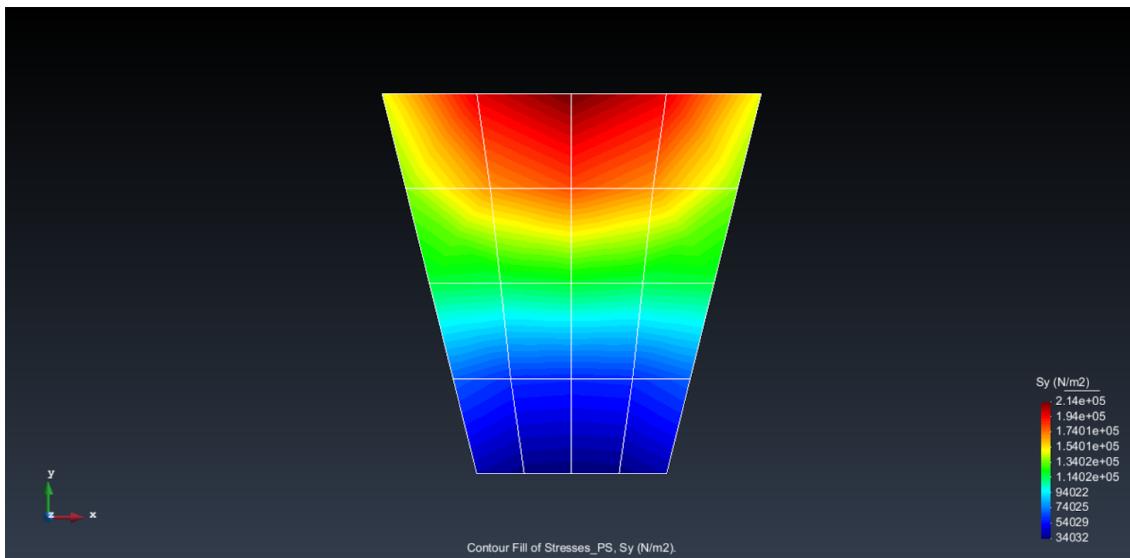


6-NODE TRIANGULAR:

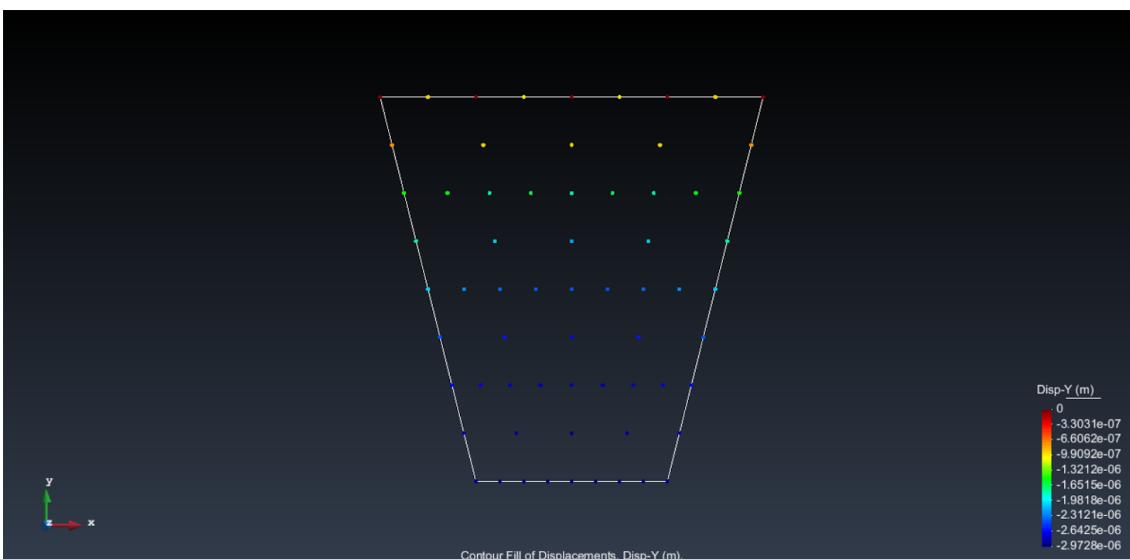


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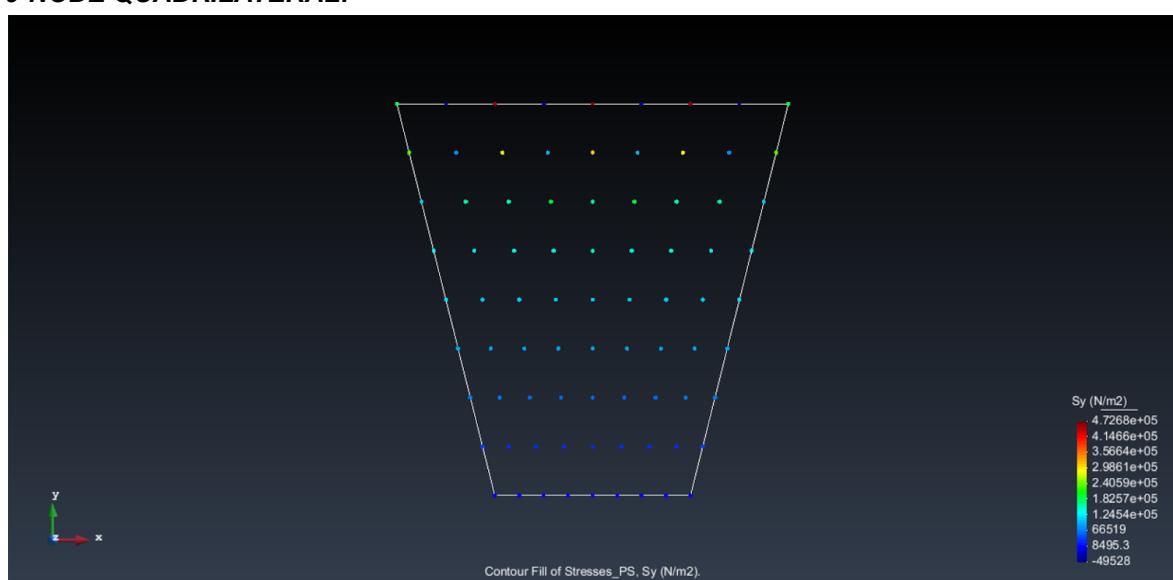
4-NODE QUADRILATERAL:



8-NODE QUADRILATERAL:



9-NODE QUADRILATERAL:



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RESULTS

Comparison is with Exact Solution,
 Point B, $\sigma_y = 2,47 \times 10^5 \text{ N/m}^2$
 Center of ED SIDE y-displ. = $2,26 \times 10^{-6} \text{ m}$

| ELEMENT TYPE | $\sigma_y^1 [\text{N/m}^2]$ | $\sigma_y^2 [\text{N/m}^2]$ | $\sigma_y^3 [\text{N/m}^2]$ |
|----------------------|-----------------------------|-----------------------------|-----------------------------|
| 3-node Triangle | 2,09E+05 | 2,24E+05 | 3,08E+05 |
| 6-node Triangle | 2,55E+05 | 2,63E+05 | 5,83E+05 |
| 4-node quadrilateral | 2,14E+05 | 2,32E+05 | 4,82E+05 |
| 8-node quadrilateral | 3,18E+05 | 4,26E+05 | 8,85E+05 |
| 9-node quadrilateral | 4,73E+05 | 5,94E+05 | 1,13E+06 |
| ELEMENT TYPE | $\delta^1 [\text{m}]$ | $\delta^2 [\text{m}]$ | $\delta^3 [\text{m}]$ |
| 3-node Triangle | 2,30E-06 | 2,29E-06 | 2,75E-06 |
| 6-node Triangle | 2,90E-06 | 3,01E-06 | 3,56E-06 |
| 4-node quadrilateral | 2,31E-06 | 2,30E-06 | 3,00E-06 |
| 8-node quadrilateral | 2,97E-06 | 3,26E-06 | 3,66E-06 |
| 9-node quadrilateral | 3,33E-06 | 3,45E-06 | 3,84E-06 |

| ELEMENT TYPE | $\varepsilon_\sigma^{\text{MESH1}} \%$ | $\varepsilon_\sigma^{\text{MESH2}} \%$ | $\varepsilon_\sigma^{\text{MESH3}} \%$ | $\varepsilon_\delta^{\text{MESH1}} \%$ | $\varepsilon_\delta^{\text{MESH2}} \%$ | $\varepsilon_\delta^{\text{MESH3}} \%$ |
|----------------------|--|--|--|--|--|--|
| 3-node Triangle | 84,62% | 90,88% | 124,77% | 101,83% | 101,44% | 121,66% |
| 6-node Triangle | 103,25% | 106,66% | 236,16% | 128,47% | 133,40% | 157,45% |
| 4-node quadrilateral | 86,64% | 94,09% | 195,11% | 102,20% | 101,78% | 132,72% |
| 8-node quadrilateral | 128,85% | 172,52% | 358,48% | 131,54% | 144,06% | 162,09% |
| 9-node quadrilateral | 191,37% | 240,48% | 459,03% | 147,28% | 152,73% | 170,09% |