

# Computational Structural Mechanics & Dynamics

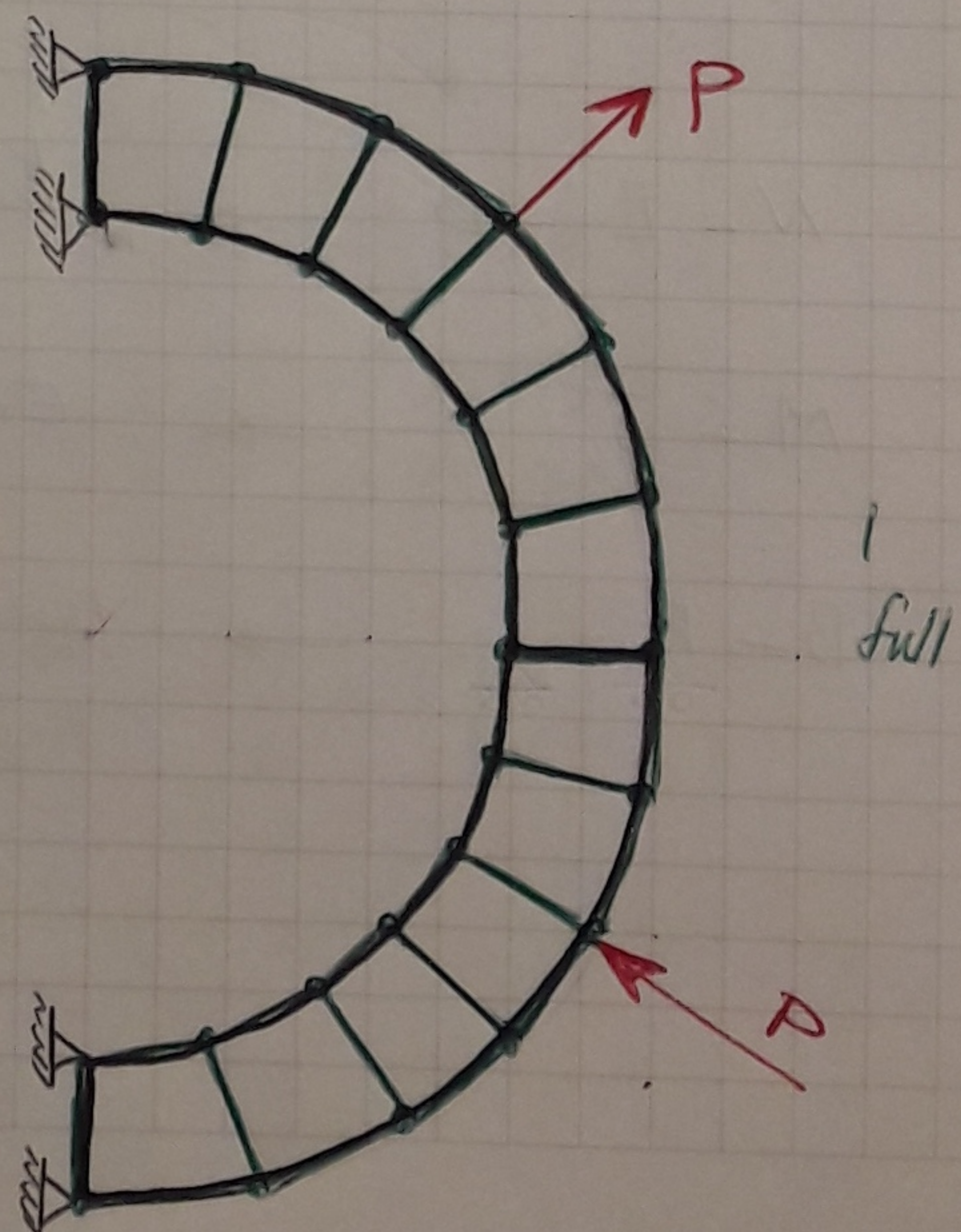
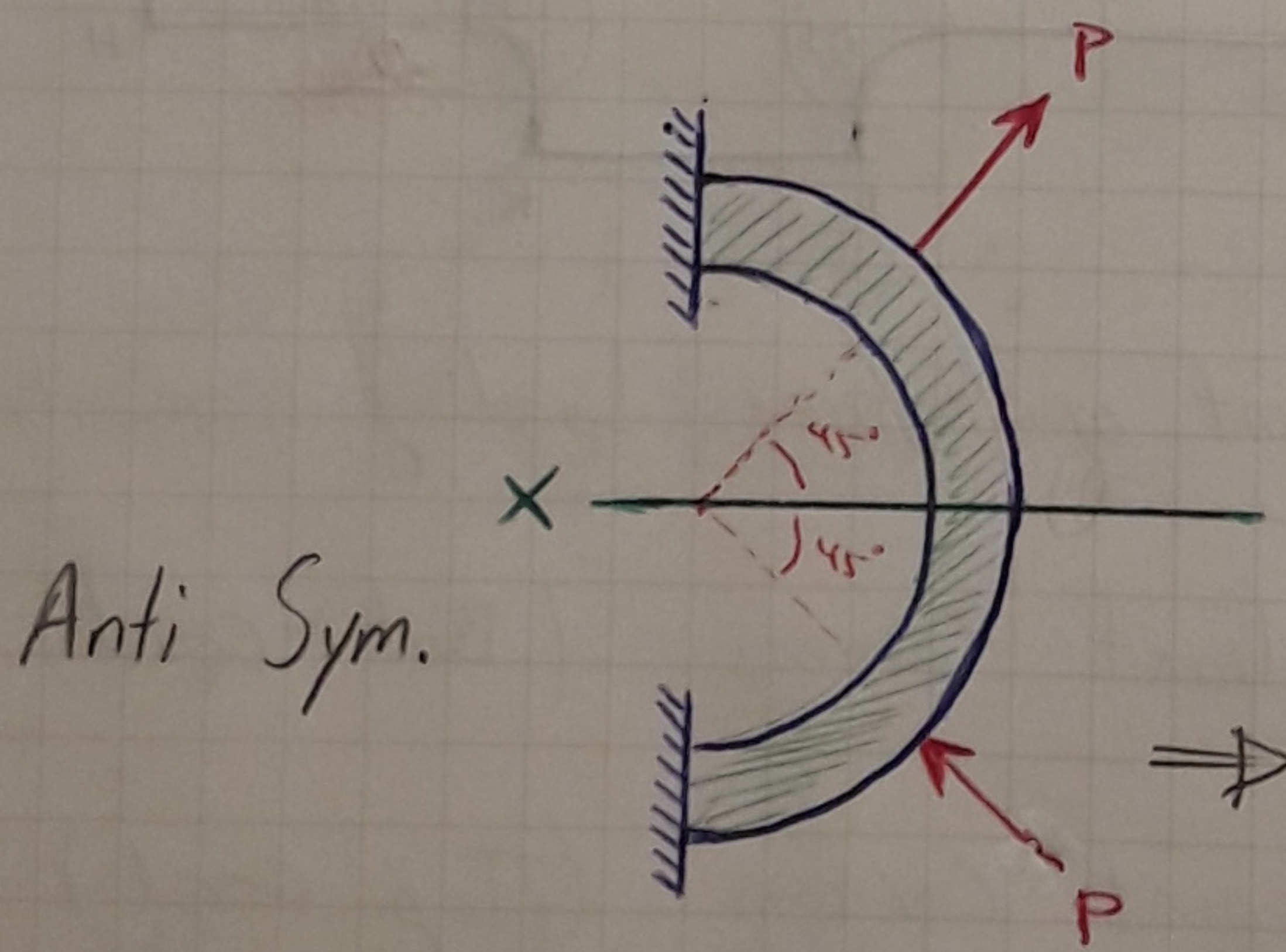
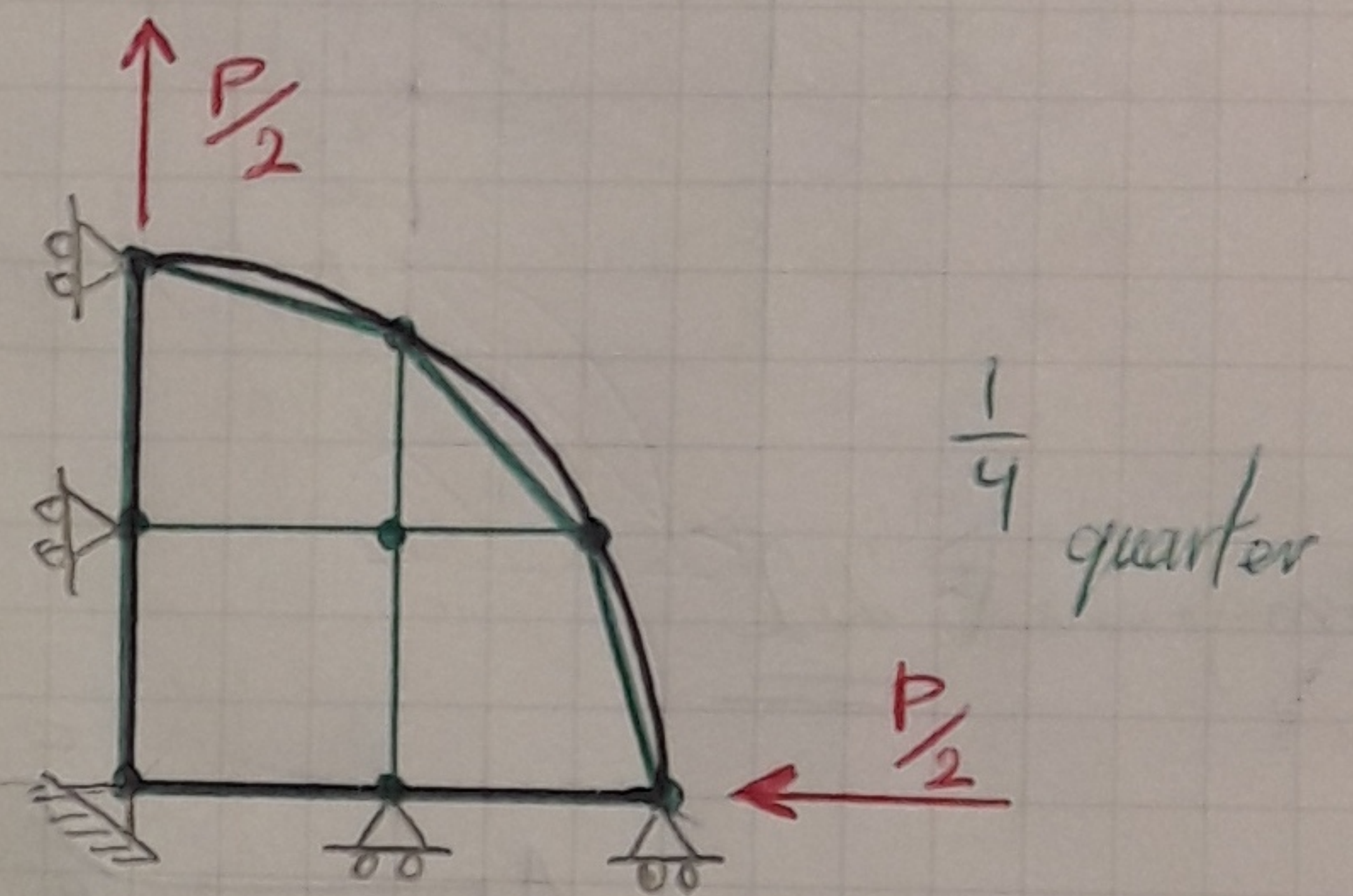
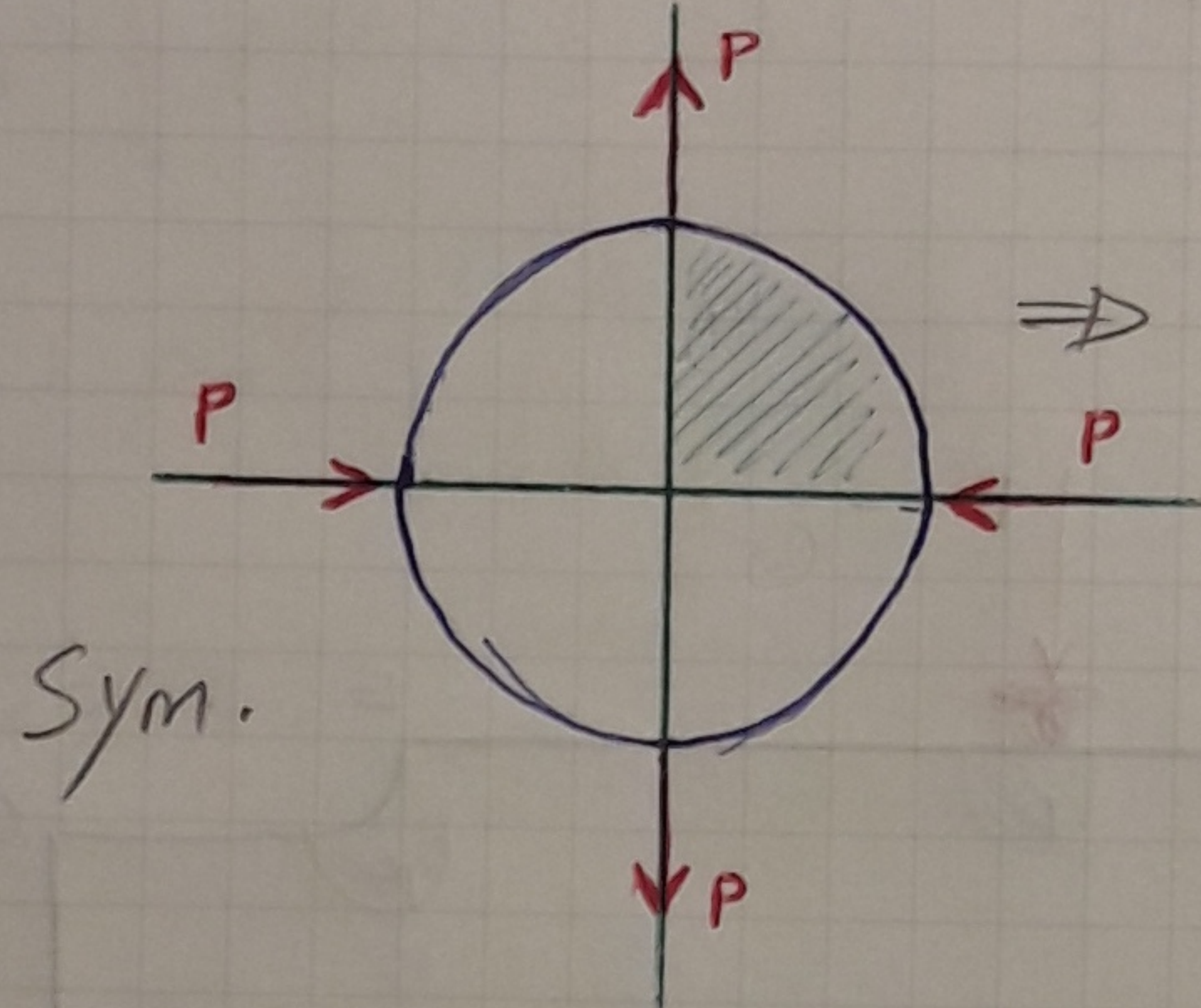
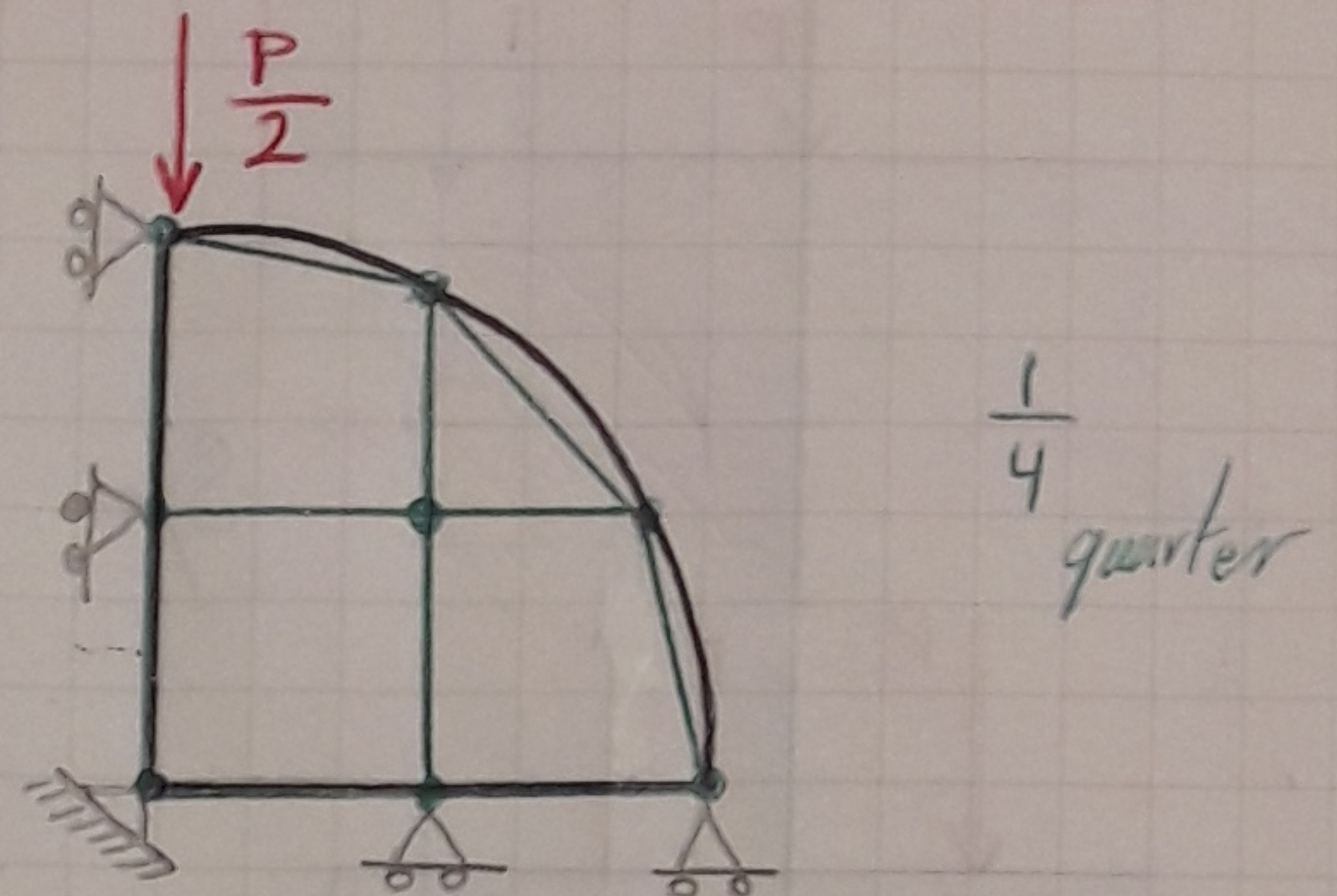
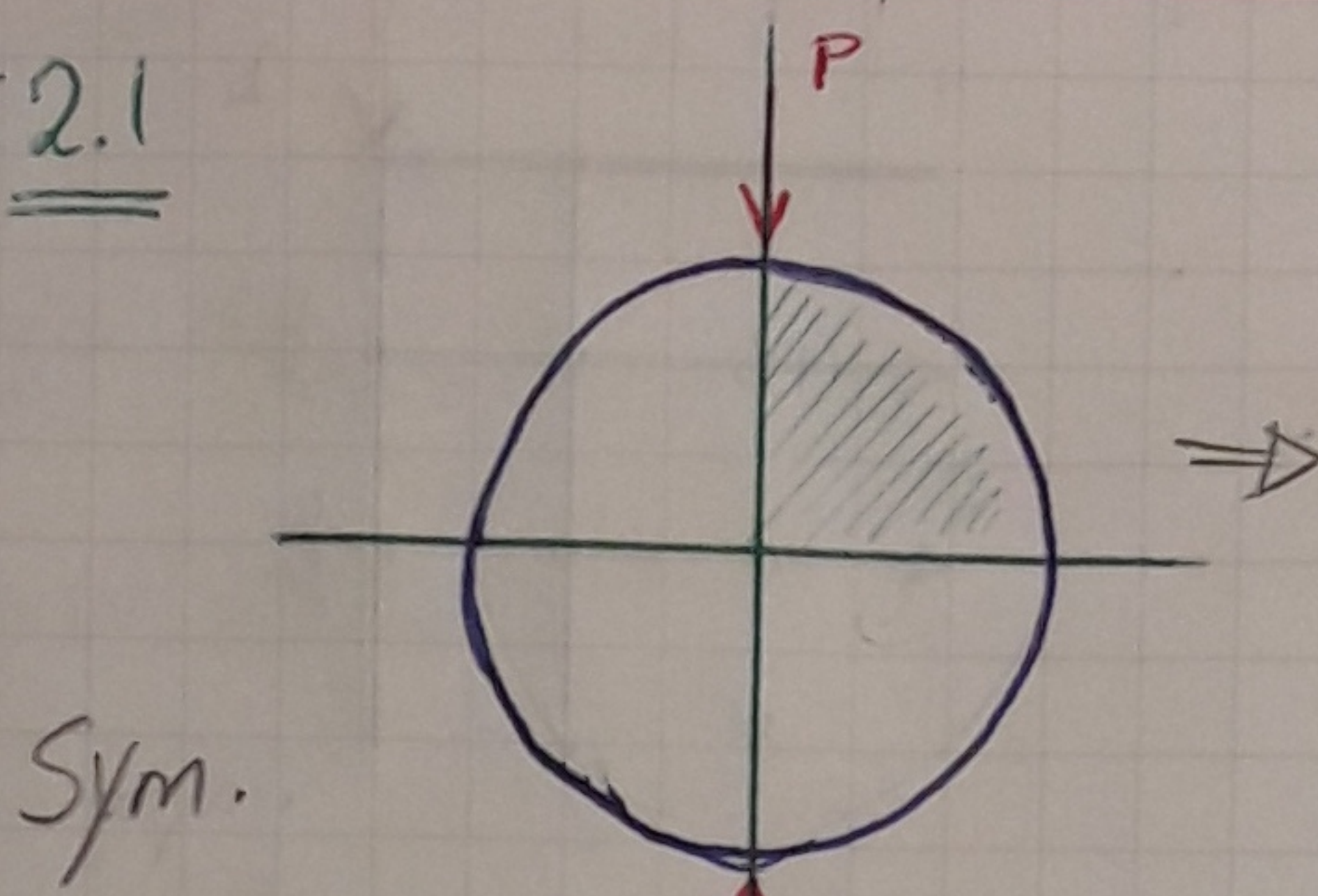
M. Mohsen Zadehkamand

Assignment 2.1 - 2.2 - 2.3

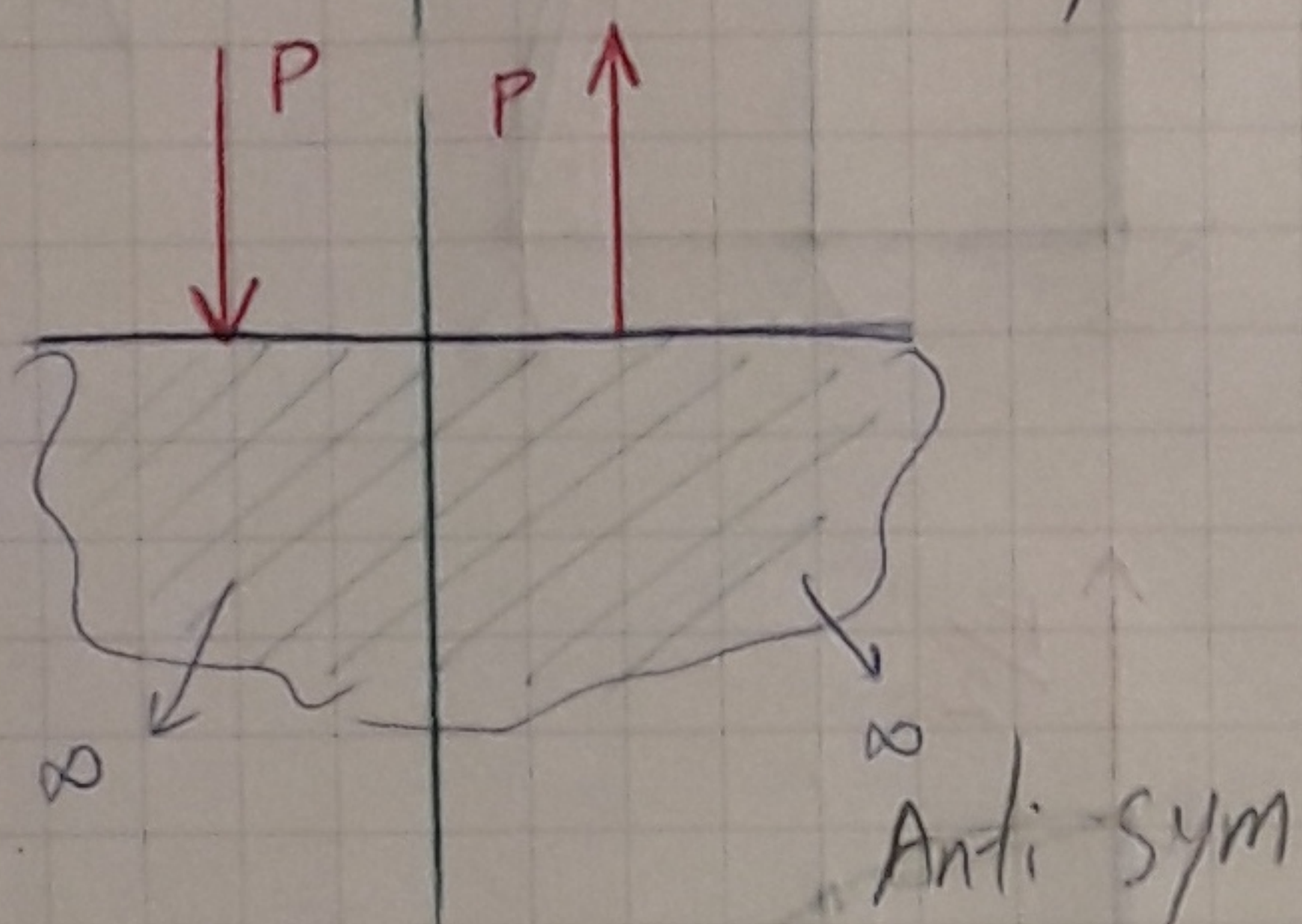
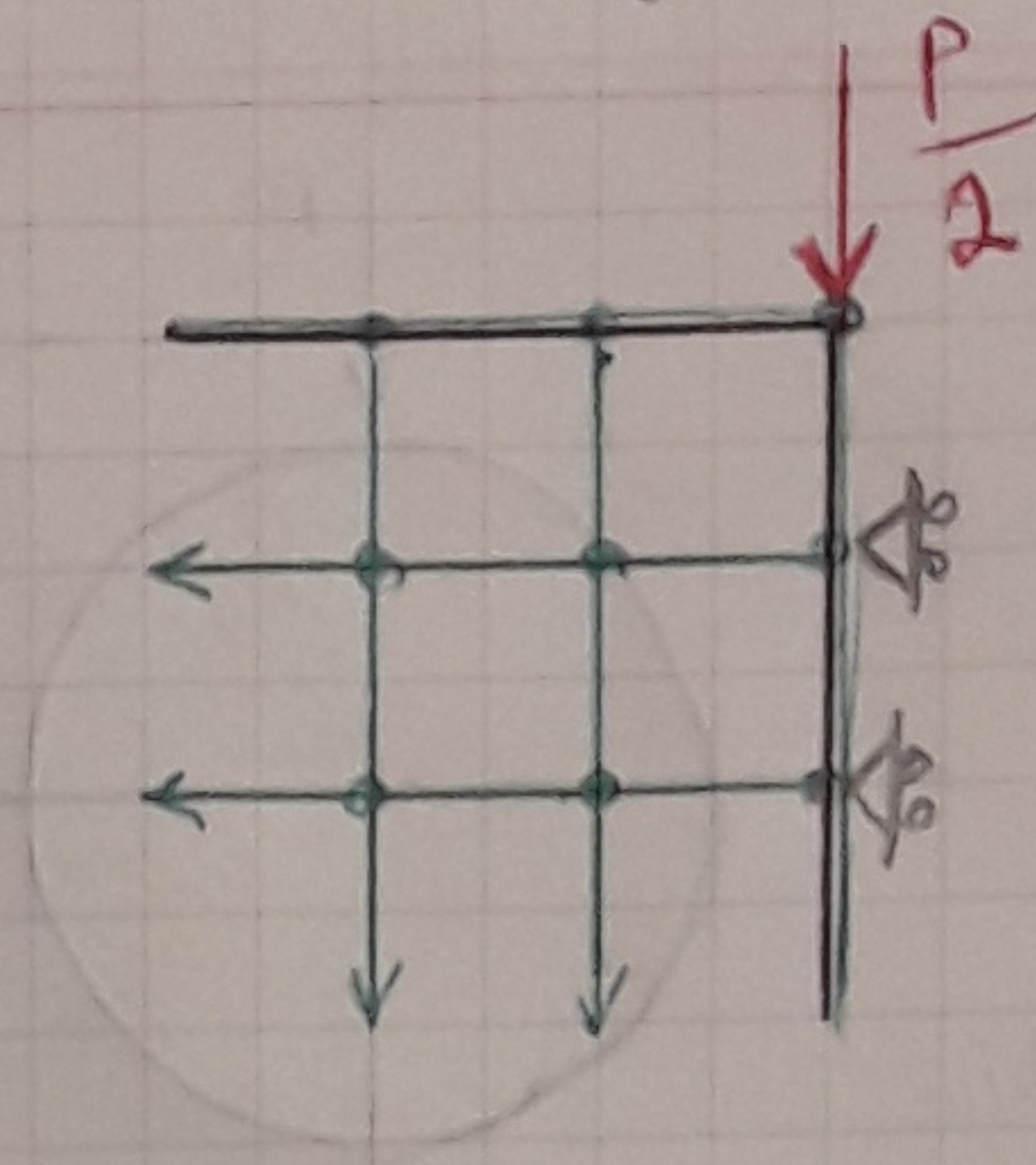
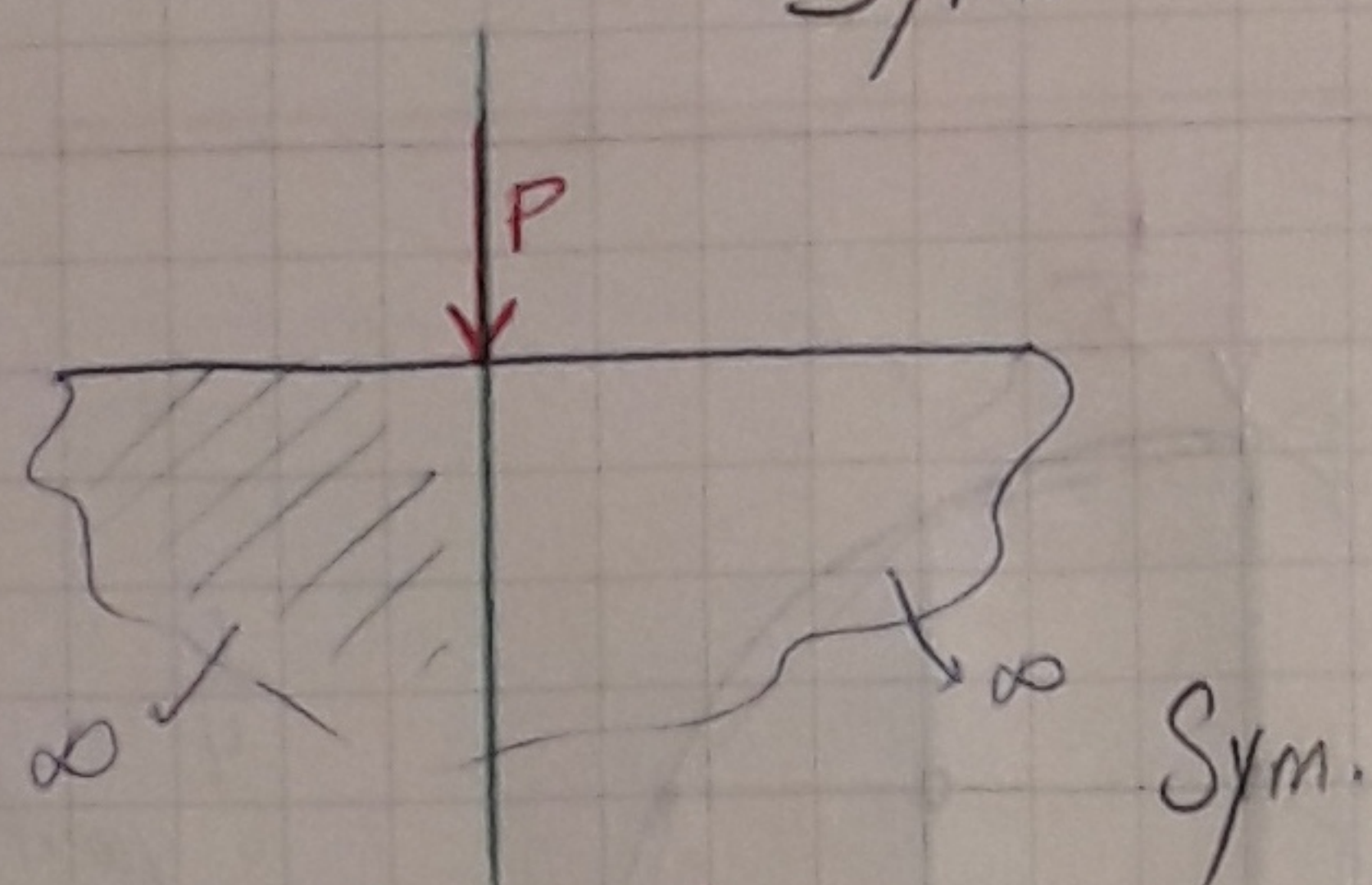
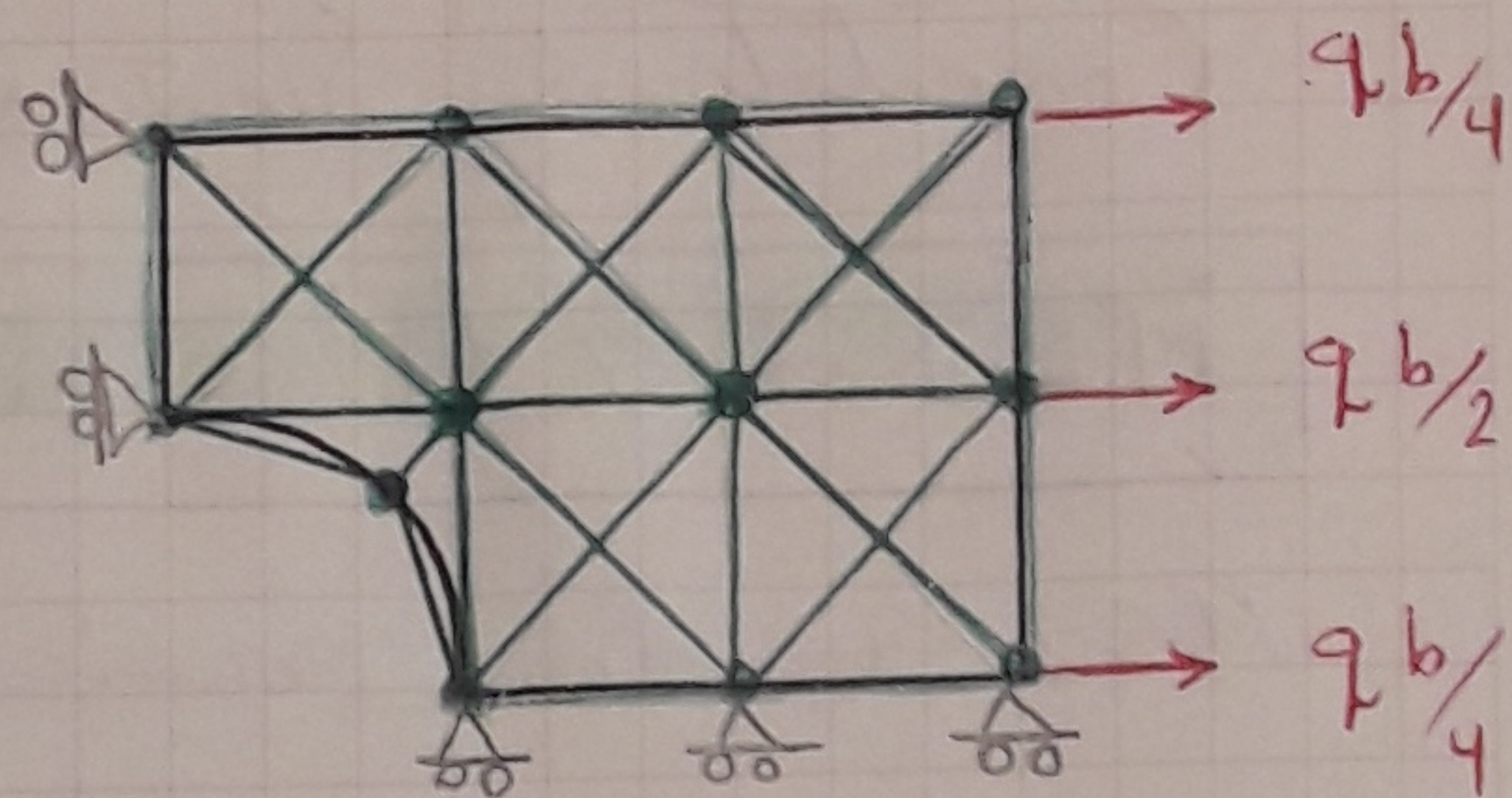
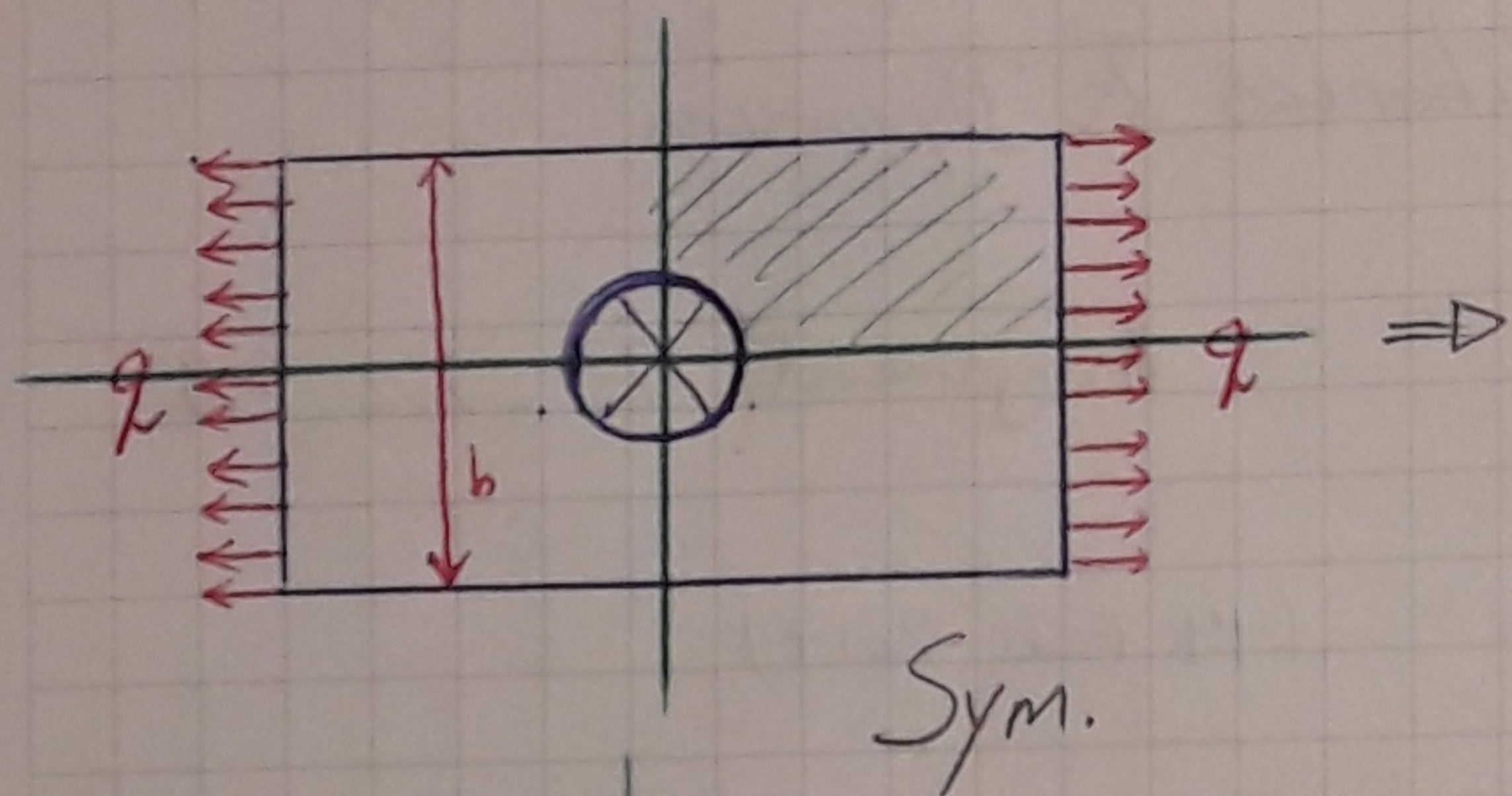
M.Sc. Computational Mechanics (2017)

(19 Feb 2017)

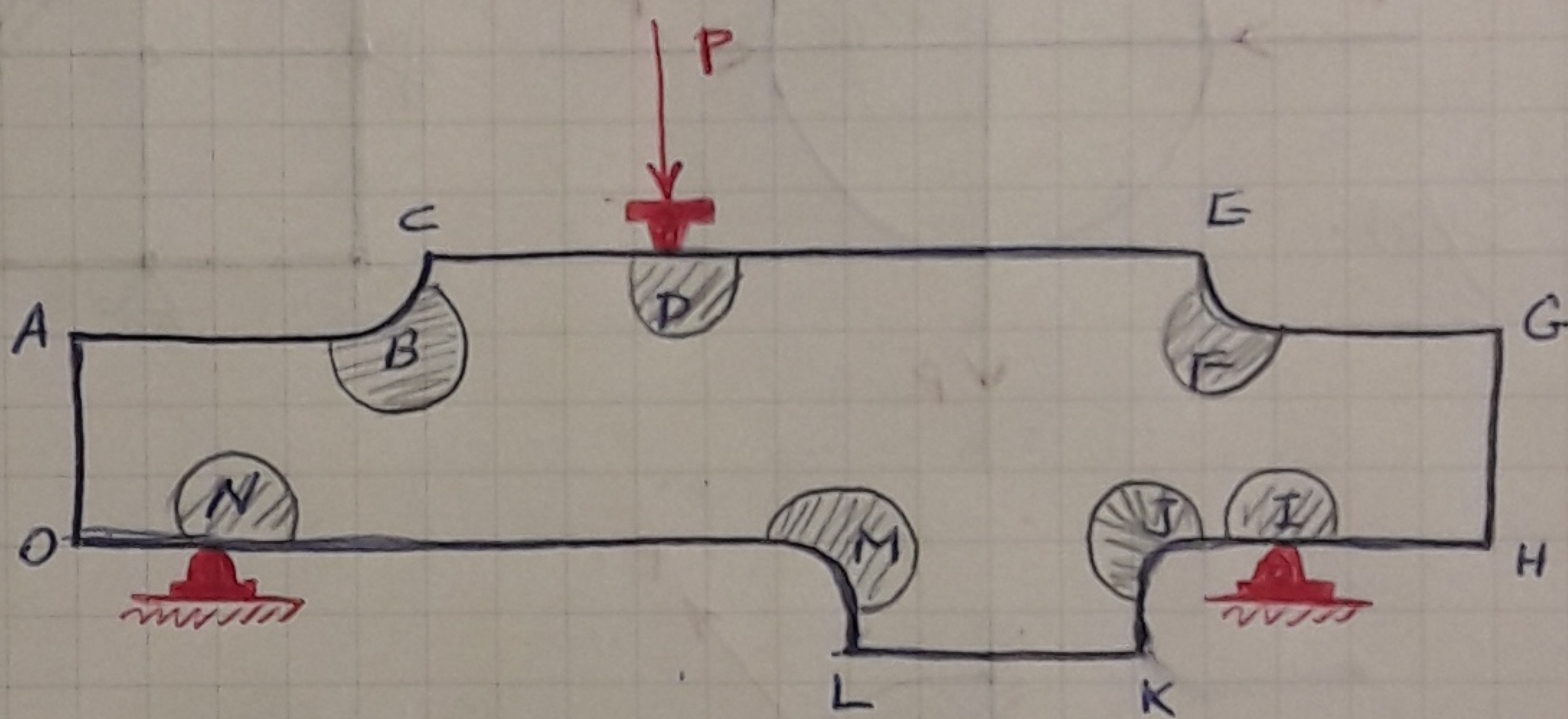
## Assignment 2.1







Assignment 2.2



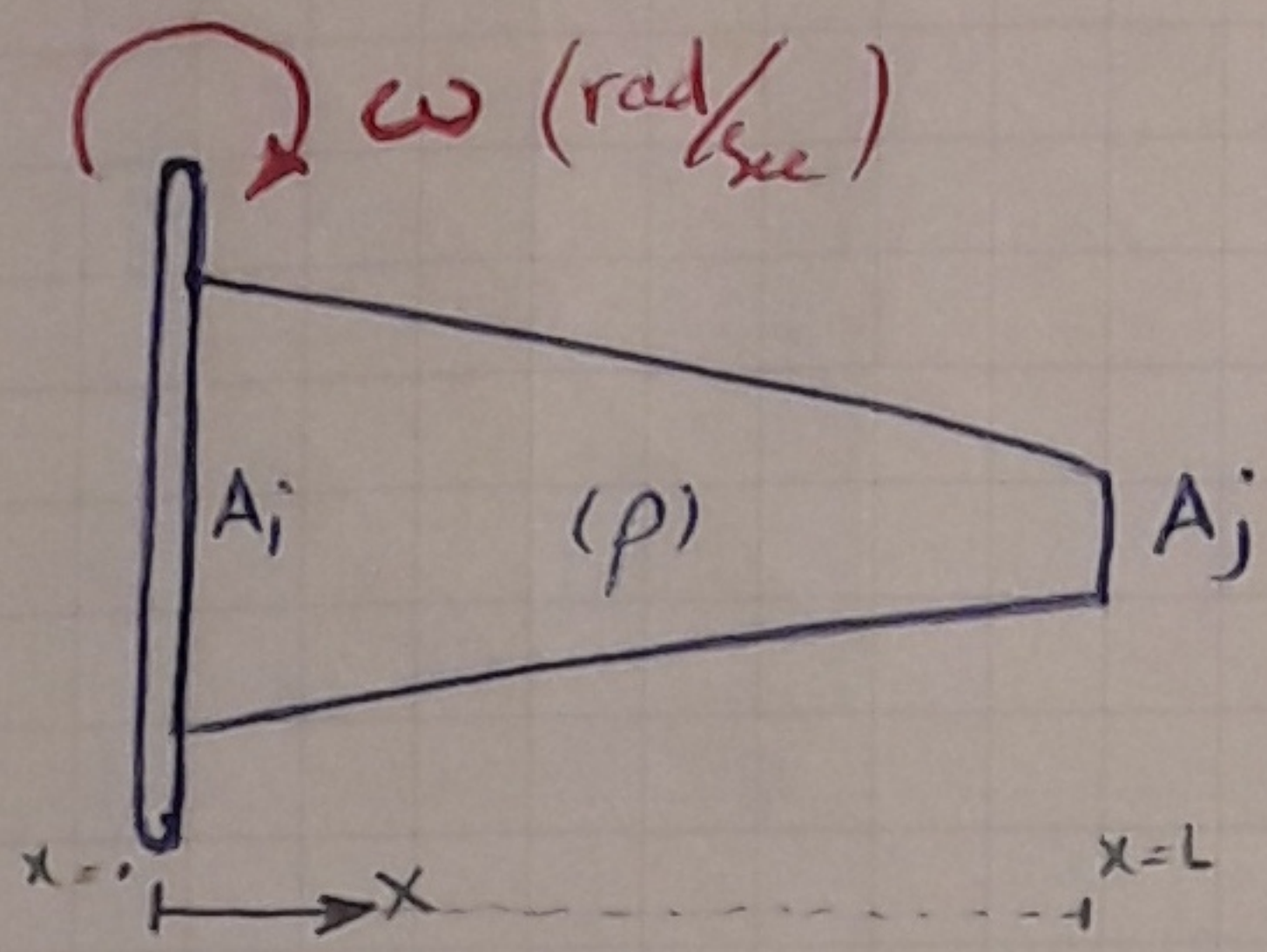
N - I - D → Point or Restrain Loading (consentrated)

M - J → Entrant Corners (Bot cord)

B - F → Entrant Corners (Top cord)



Assignment 2-3 Variational Formulation.



$$A = A_i (1 - \xi) + A_j \xi$$

$$q(x) = \rho A \omega^2 x$$

$$W = \int_0^L q u \, dx$$

$$W^e = \int_0^1 q (W^T u^e) (l \, d\xi)$$

$$W^e = (u^e)^T \int_0^1 q \begin{bmatrix} 1 - \xi \\ \xi \end{bmatrix} l \, d\xi$$

$$\Rightarrow f_{\text{ext}} = \int_0^1 \rho (A_i (1 - \xi) + A_j \xi) \omega^2 \xi l \begin{bmatrix} 1 - \xi \\ \xi \end{bmatrix} l \, d\xi$$

$$= \rho \omega^2 l^2 \int_0^1 \begin{bmatrix} A_i \xi (1 - \xi)^2 + A_j \xi^2 (1 - \xi) \\ A_i \xi^2 (1 - \xi) + A_j \xi^3 \end{bmatrix} d\xi$$

$$= \rho \omega^2 l^2 \int_0^1 \begin{bmatrix} A_i (\xi^3 + \xi - 2\xi^2) + A_j (\xi^2 - \xi^3) \\ A_i (\xi^2 - \xi^3) + A_j \xi^3 \end{bmatrix} d\xi$$

$$= \rho \omega^2 l^2 \left[ \begin{array}{l} A_i \left( \frac{\xi^4}{4} + \frac{\xi^2}{2} - \frac{2}{3} \xi^3 \right) + A_j \left( \frac{\xi^3}{3} - \frac{\xi^4}{4} \right) \\ A_i \left( \frac{\xi^3}{3} - \frac{\xi^4}{4} \right) + A_j \frac{\xi^4}{4} \end{array} \right]_0^1$$

$$= \rho \omega^2 l^2 \left[ \begin{array}{l} A_i \left( \frac{1}{4} + \frac{1}{2} - \frac{2}{3} \right) + A_j \left( \frac{1}{3} - \frac{1}{4} \right) \\ A_i \left( \frac{1}{3} - \frac{1}{4} \right) + A_j \frac{1}{4} \end{array} \right] = \rho \omega^2 l^2 \left[ \begin{array}{l} \frac{1}{12} A_i + \frac{1}{12} A_j \\ \frac{1}{12} A_i + \frac{1}{4} A_j \end{array} \right]$$

$$= \frac{1}{12} \rho \omega^2 l^2 \begin{bmatrix} A_i + A_j \\ A_i + 3A_j \end{bmatrix}$$

if  $A = A_i = A_j \rightarrow f_{\text{ext}} = \begin{bmatrix} f_0 \\ f_1 \end{bmatrix} = \frac{1}{12} \rho \omega^2 l^2 \begin{bmatrix} 2A \\ 4A \end{bmatrix} = \frac{1}{6} \rho \omega^2 l^2 \begin{bmatrix} A \\ 2A \end{bmatrix}$

